

$$\rightarrow \sum_i \left( -\frac{\hbar^2}{2m} \nabla_i^2 \right) + \sum_i \sum_j \left( \frac{Z+1)e}{4\pi\epsilon_0 |R_a - R_b|} \right) + \sum_i \sum_j \left( \frac{e^2}{4\pi\epsilon_0 |r_i - r_j|} \right)$$

$$E = \langle \phi(x_1 \dots x_N) | H | \phi(x_1 \dots x_N) \rangle$$

$$h = -\frac{\hbar^2}{2m} \nabla^2 + \sum_j \frac{Z+1)e}{4\pi\epsilon_0 |R_a - R_b|} + \sum_j \left( \frac{e^2}{4\pi\epsilon_0 |r_i - r_j|} \right)$$

$$\frac{1}{\sqrt{N!}} \begin{pmatrix} \phi_1(x_1) \phi_2(x_1) \dots \phi_N(x_1) \\ \vdots \\ \phi_N(x_N) \phi_N(x_N) \dots \phi_N(x_N) \end{pmatrix}$$

$$h\phi(r) = \sum_i \epsilon_i \phi_i(r)$$

$$\rightarrow \sum_n^k c_n b_n(r)$$

$$\begin{pmatrix} \langle b_1 | h | b_1 \rangle \dots \langle b_k | h | b_1 \rangle \\ \vdots \\ \langle b_1 | h | b_k \rangle \dots \langle b_k | h | b_k \rangle \end{pmatrix}$$

$$x \begin{pmatrix} c_1 \\ \vdots \\ c_k \end{pmatrix} = \epsilon_i \begin{pmatrix} \langle b_1 | b \rangle \dots \langle b_1 | b \rangle \\ \vdots \\ \langle b_k | b \rangle \dots \langle b_k | b \rangle \end{pmatrix}$$

Many body

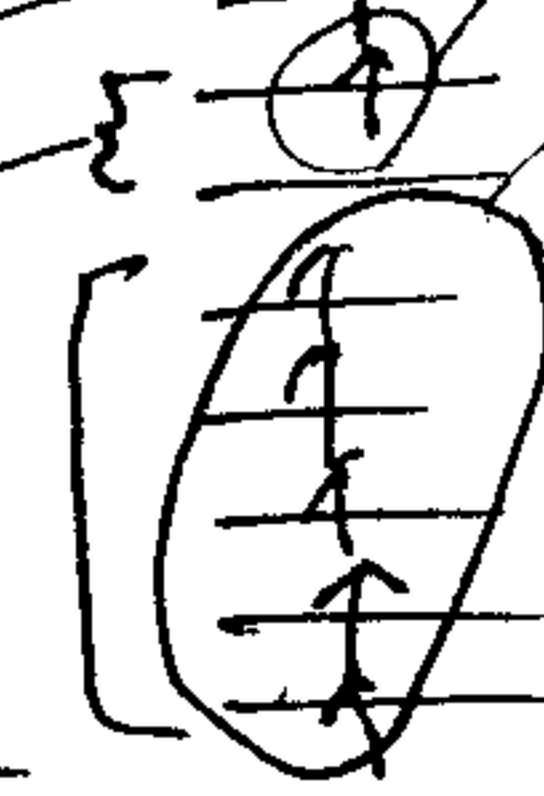
Single body

Virtual occupied.

HF = N-body solution.

(바탕 함수가 겹침)  
energy band gap  
= 가동 overlap + 교환  
but exchange  
효과

K



$$C_0 \phi(x_1 \dots x_N) + C_1 \phi'(x_1 \dots x_N)$$

$$C_0 = 2, C_1 = 0$$

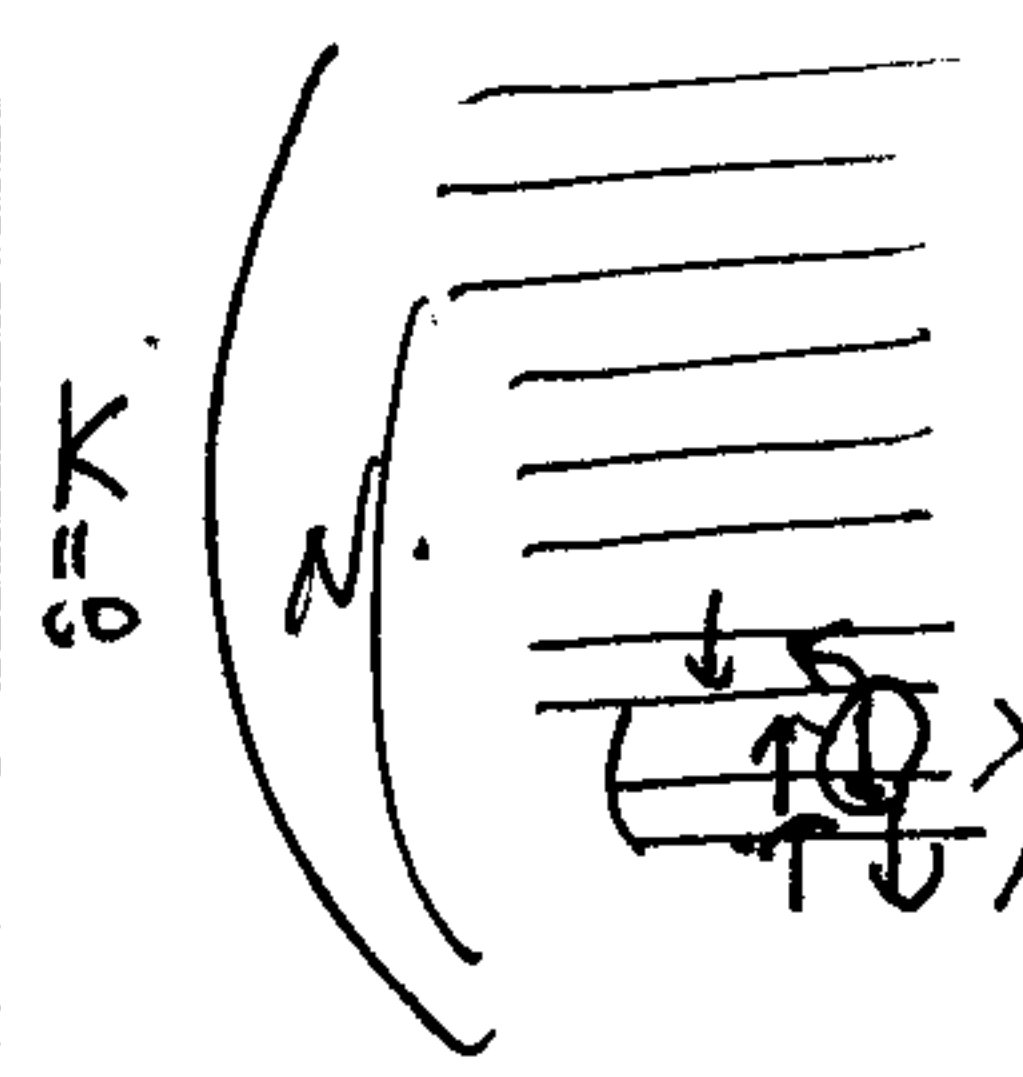
$$\phi = \sum c_n^{(k)} b_n(r)$$

linear combination  
E가 여러  
configuration

파동function 형태는 N개  
자른 양자 N-H state 여러 linear combination  
(virtual orbital 같은 base set 같은 것 같을  
것 같은 것 C 가 여러)  
HF ⇒ base set 같은 것 of many body

HF 근사해서 보면

$$\psi = \int_K d\mathbf{k} \phi_{\mathbf{k}}^{(k)}(x_1 \dots x_N)$$



$$4C_1 C_2 \dots C_{(K-N)} C_1$$

(i) 1개 취할 양자  
⇒  $\phi_1^k$  ; 1개 ↓  
(ii) 2개 취할 양자 ⇒  
 $N C_2 (2K-N) C_2$   
↓  
Pauli 배타원리  
위해.

antisymmetry many body.

$$\int \frac{\det}{\sqrt{N!}} \begin{pmatrix} \phi_1^*(x_1) \phi_2^*(x_1) \dots \phi_N^*(x_1) \\ \vdots \\ \phi_1^*(x_N) \phi_2^*(x_N) \dots \phi_N^*(x_N) \end{pmatrix} \frac{\det}{\sqrt{N!}} \begin{pmatrix} \phi_1(x_1) \dots \phi_N(x_1) \\ \vdots \\ \phi_1(x_N) \dots \phi_N(x_N) \end{pmatrix} d(x_1 \dots x_N)$$

$$\frac{1}{\sqrt{N!}} \begin{pmatrix} \phi_1(x_1) \dots \phi_N(x_1) \\ \vdots \\ \phi_N(x_N) \dots \phi_N(x_N) \end{pmatrix}$$

$$\begin{pmatrix} \langle \phi^1 | H | \phi^1 \rangle \langle \phi^2 | H | \phi^2 \rangle \dots \langle \phi^k | H | \phi^k \rangle \\ \vdots \\ \langle \phi^1 | H | \phi^k \rangle \dots \langle \phi^k | H | \phi^k \rangle \end{pmatrix}$$

$$\begin{pmatrix} \langle \phi^1 | \phi^1 \rangle \langle \phi^1 | \phi^2 \rangle \dots \langle \phi^1 | \phi^k \rangle \\ \vdots \\ \langle \phi^k | \phi^k \rangle \dots \end{pmatrix} \begin{pmatrix} d_1 \\ \vdots \\ d_k \end{pmatrix}$$

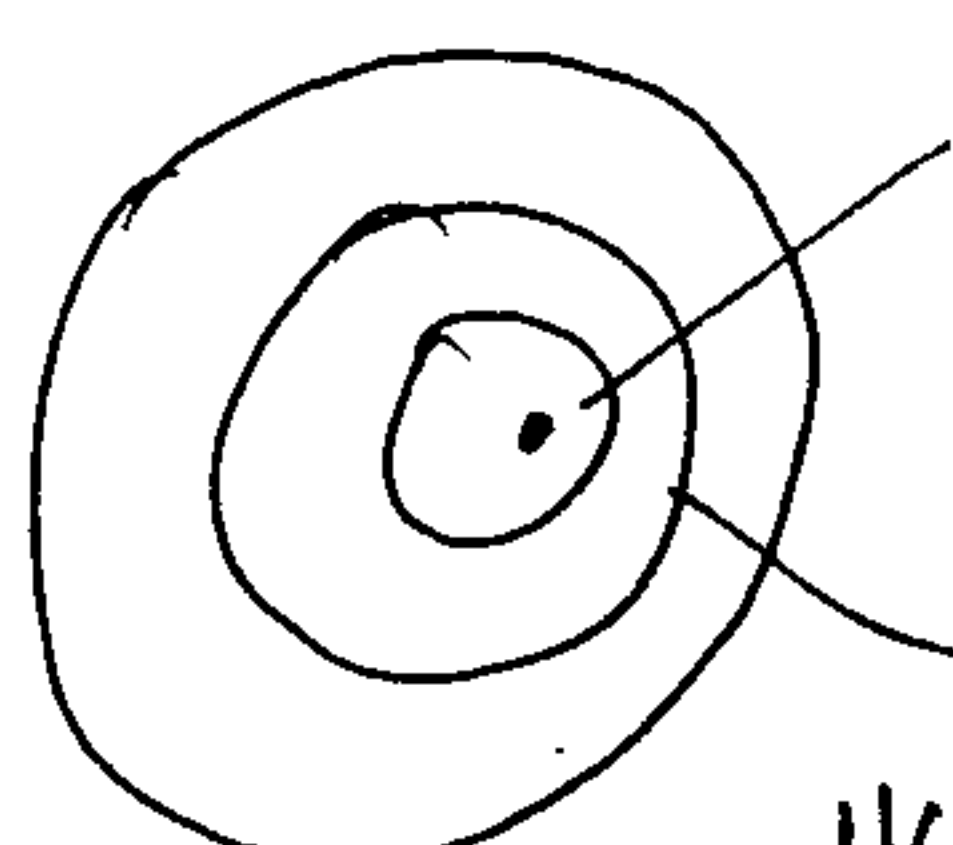
$$\psi_0 = \frac{1}{\sqrt{2}} \begin{pmatrix} \phi_1(x_1) \phi_2(x_1) \\ \phi_1(x_2) \phi_2(x_2) \end{pmatrix}$$

$$\psi_1 = \frac{1}{\sqrt{2}} \begin{pmatrix} \phi_1(x_1) \phi_2(x_2) \\ \phi_1(x_2) \phi_2(x_1) \end{pmatrix}$$

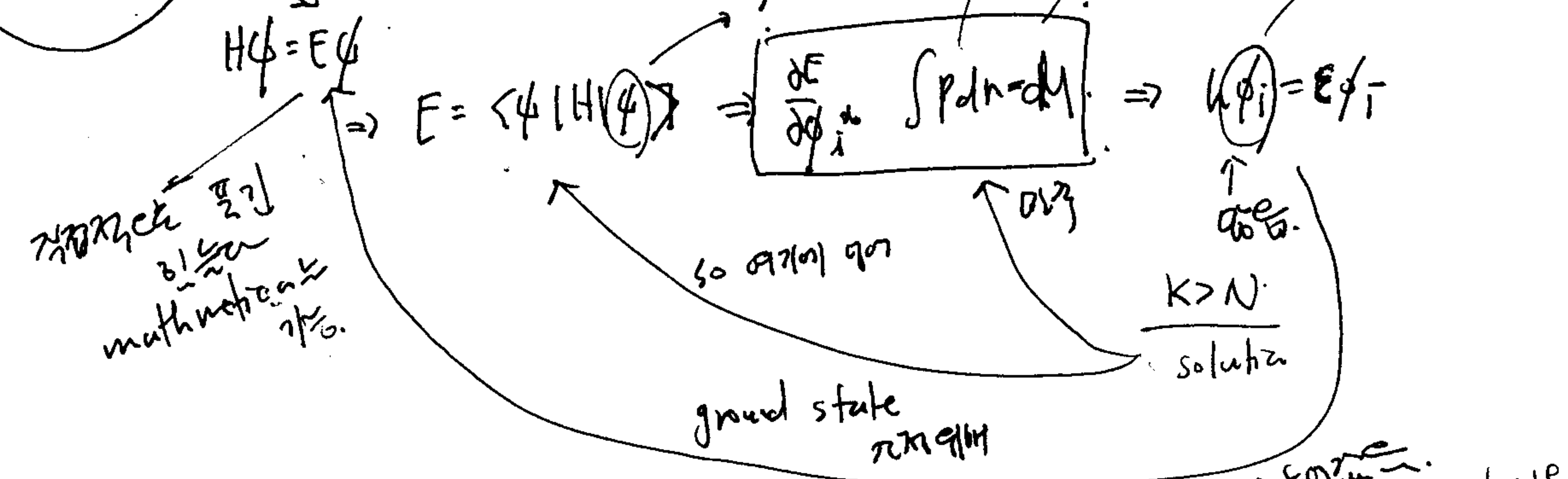
$$\psi_2 = \frac{1}{\sqrt{2}} \begin{pmatrix} \phi_1(x_1) \phi_2(x_1) \\ \phi_1(x_2) \phi_2(x_2) \end{pmatrix}$$

5-N

$(\psi_5 \psi_7)$  ...  $\rightarrow$  infinite full CI? 이쯤만 있는 거야.



system with force antisymmetry



$L = \infty$  full CI.  
(Configuration Interaction)

$$\rho(r) = \frac{1}{\text{Norm.}} \sum_{\alpha=1}^N \phi_{\alpha}^*(r) \phi_{\alpha}(r)$$

$$\int \rho(r) dr = \sum_{\alpha=1}^N \int \phi_{\alpha}^* \phi_{\alpha}(r) dr = \sum_{\alpha=1}^N 1 = N$$